

# How I spent last summer

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October 17, 2023

## Abstract

In this article, I shall discuss how I spent last summer.

## Introduction

Preparation is described in Section 1, beginning in Section 2, and summer proper in Section 3. Section 4 contains a photo showing a capybara that I saw when I visited the capybara cafe in Tokyo.

*Note: Everything written about in this document is entirely fictional and not intentionally based on any true events.*

## 1 Preparation

Prepare for summer:

1. Get fit
  - (a) Jogging
  - (b) Press-ups
  - (c) Learn to swim
2. Buy summer clothes
3. Buy tickets

## 2 May

Apart from recreational activities, in May I also did some maths, as described in Subsection 2.3.

## 2.1 May weather

It was raining *a lot*. This phenomenon is explained in [1, Section 4].

## 2.2 Reading books

Because of what is described in Subsection 2.1, we stayed indoors and read the book [2].

## 2.3 Maths

I was also revising some maths for A-level exams, like the following.

**Theorem 1.** *The solutions of a quadratic equation  $ax^2 + bx + c = 0$  are given by the formulae*

$$x_1 = \frac{-b + \sqrt{b^2 - 4ac}}{2a} \quad \text{and} \quad x_2 = \frac{-b - \sqrt{b^2 - 4ac}}{2a}.$$

**Lemma 1.** *A finite sum  $\sum_{i=0}^k r^i a_0$  of a geometric progression with ratio  $r \neq 1$  is equal to*

$$a_0 \left( \frac{1 - r^{k+1}}{1 - r} \right).$$

*Proof.* We have

$$(1 - r)(1 + r + r^2 + \cdots + r^k) = 1 - r^{k+1},$$

which is verified by expanding brackets:

$$\begin{aligned} (1 + r + r^2 + \cdots + r^k) - r(1 + r + r^2 + \cdots + r^k) \\ = 1 + r + r^2 + \cdots + r^k - r - r^2 - \cdots - r^k - r^{k+1} = 1 - r^{k+1}. \end{aligned}$$

Dividing both sides of formula (3) by  $r - 1$  and multiplying by  $a_0$  we have

$$a_0 + ra_0 + r^2a_0 + r^3a_0 + \cdots + r^ka_0 = a_0 \left( \frac{1 - r^{k+1}}{1 - r} \right).$$

□

**Theorem 2.** *The infinite sum  $\sum_{i=0}^{\infty} r^i a_0$  of a geometric progression with ratio  $r$  satisfying  $0 < r < 1$  is equal to  $\frac{a_0}{1-r}$ .*

*Proof.* The sum  $\sum_{i=0}^{\infty} r^i a_0$  is equal to the limit of the partial sums  $\sum_{i=0}^k r^i a_0$  as  $k$  tends to  $\infty$ . By Lemma 1,

$$\sum_{i=0}^k r^i a_0 = a_0 \left( \frac{1 - r^{k+1}}{1 - r} \right).$$

When  $0 < r < 1$ , the term  $r^{k+1}$  tends to 0 as  $k$  tends to  $\infty$ . Hence the result. □

### 3 Summer proper

After exams, we watched football matches on TV. At the moment the table in group E looks as in Table 1.

Table 1: Euro 2016. Group E

| Pos | Team                | Pld | W | D | L | GD | Pts | Qualification |
|-----|---------------------|-----|---|---|---|----|-----|---------------|
| 1   | Italy               | 3   | 2 | 0 | 1 | +2 | 6   | Qualified     |
| 2   | Belgium             | 3   | 2 | 0 | 1 | +2 | 6   | Qualified     |
| 3   | Republic of Ireland | 3   | 1 | 1 | 1 | 0  | 4   | Round of 16   |
| 4   | Sweden              | 3   | 0 | 1 | 2 | -2 | 1   |               |

### 4 Photo

Figure 1 shows the capybara cafe from Tokyo



Figure 1: Capybara Cafe

### References

- [1] A. Nother, Recent advances in weather prediction, *J. Adv. Weather* **76**, no. 3 (2013), 23-45.

- [2] S. Someone, *A great book*, Lincoln, 2014.
- [3] C. Capybara, Cafe Capybara introduction page, *Cafe Capybara*, 2023.